

Review What You Know!

Vocabulary

Choose the best term from the box.

- algebraic expression
- equation
 variable
- **1.** 3x = 15 is a(n) ?.
- **2.** 3*x* is a(n) <u>?</u>.
- **3.** In 3*x*, *x* is the <u>?</u>.

Rules and Tables

Write the rule using words, and then with a variable.

4.	in	out	5.	in	out
	36	6		5	12
	42	7		10	17
	48	8		15	22

Fractions

Write the fraction. Simplify if necessary.

- **6.** If 2 out of 4 bananas are green, what fraction names the green bananas?
- 7. If $\frac{5}{6}$ of a loaf of bread is eaten, what part of the loaf is NOT eaten?

Multiplying Factors

Writing to Explain Write an answer to the question.

 Clint bought 3 T-shirts at \$9 each and 2 pairs of shorts at \$12 each. Explain how to find the total Clint spent.

What shape do these wasps create when they build their hive? You will find out in Lesson 8-3.

4

What kinds of angles are formed by the handles of the world's largest basket? You will find out in Lesson 8-2.







MG 2.1 Come Measure, identify, and draw angles, perpendicular and parallel lines, rectangles, and triangles by using appropriate tools (e.g., straightedge, ruler, compass, protractor, drawing software).

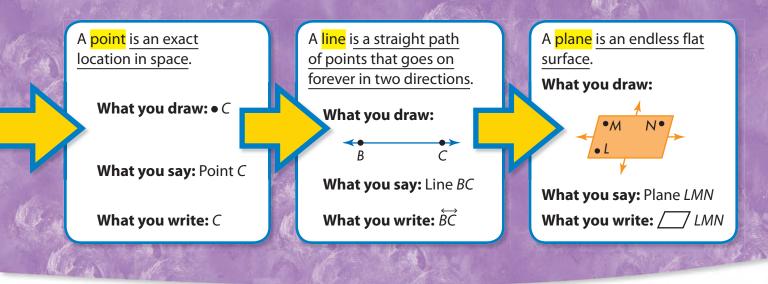
Basic Geometric Ideas

How can you describe locations and parts of space?

Points, lines, and planes are basic geometric concepts. Engineers and architects use these concepts in designing streets, buildings, and structures.

Other Examples

	What You Draw	What You Say	What You Write
A <mark>line segment</mark> is part of a line and has 2 endpoints.	R S	Line segment RS	RS
A <mark>ray</mark> is <u>part of a</u> line. It has only one endpoint and extends forever in one direction.	J K	Ray <i>JK</i>	JK
Parallel lines never cross and stay the same distance apart.	V W	Line <i>AD</i> is parallel to line <i>VW</i> .	$\overrightarrow{AD} \parallel \overleftarrow{VW}$
Intersecting lines pass through the same point.	P C Q E	Line <i>PE</i> intersects line <i>QC</i> .	\overleftrightarrow{PE} intersects \overleftrightarrow{QC}
Perpendicular lines are <u>intersecting lines</u> that form square corners.	F R H S This symbol means square corner or right angle.	Line <i>RS</i> is perpendicular to line <i>FH</i> .	ŔŜ⊥ĨĤ X
2. Are all perpendicul	allel or intersecting? Exp ar lines intersecting? lines perpendicular?	lain how you know.	B V Y



Guided Practice*

Do you know HOW?

- In 1 through 4, use the diagram at the right.
 - 1. Name 4 points.
 - 2. Name 3 line segments.
 - 3. Name 2 intersecting lines
 - 4. Name 2 parallel lines.

Do you UNDERSTAND?

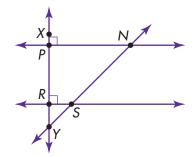
In **5** through **7** use the diagram at the left.

- **5.** If \overrightarrow{PS} and \overrightarrow{TC} are parallel and \overrightarrow{PS} is perpendicular to \overrightarrow{PT} , is \overrightarrow{TC} also perpendicular to \overrightarrow{PT} ?
- **6.** Do \overrightarrow{PS} and \overrightarrow{SP} name the same line?
- **7.** Do \overrightarrow{PS} and \overrightarrow{SP} name the same ray? Explain.

Independent Practice

In 8 through 13, use the diagram at the right.

- 8. Name two parallel lines.
- 9. Name two perpendicular lines.
- **10.** Name two intersecting but not perpendicular lines.
- **11.** Name three line segments.
- **12.** Name a plane.
- **13.** Name three rays.

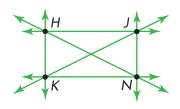




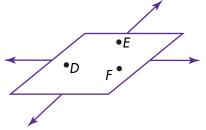


Problem Solving

14. Use the diagram below to name each of the following.



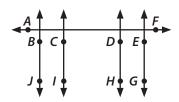
- a 2 sets of parallel lines
- **b** 2 sets of perpendicular lines
- **16. Reasoning** Points *D*, *E*, and *F* lie in plane *DEF*. How many lines in plane *DEF* can you draw that contain both points *D* and *E*?



- 18. Rover weighs 5 pounds more than the neighbor's dog. Rover is 7 years old, and the neighbor's dog is 9 years old. Together they weigh 75 pounds. How much does Rover weigh?
- **20. Writing to Explain** How are perpendicular lines like intersecting lines? What is the difference between perpendicular and intersecting lines?
- 22. In how many different ways can you arrange the books shown at the right on a shelf? Make a list of the possible ways.



- **15.** Think About the Process Minh bought 2 pounds of apples for \$0.50 a pound, and a gallon of milk for \$2. Which operations would you use to find Minh's total cost for the apples and milk?
 - A Multiply and divide
 - **B** Add and add
 - **C** Multiply and subtract
 - **D** Multiply and add
- 17. Think About the Process Joshua bought a basketball for \$22 and 3 T-shirts for \$9 each. Which expression shows how to find how much Joshua spent?
 - **A** $$22 + (3 \times $9)$
 - **B** 3 × (\$22 + \$9)
 - **C** $(3 \times $22) + (3 \times $9)$
 - **D** $(3 + $22) \times (3 + $9)$
- 19. An airplane is carrying 148 passengers. There are 110 adults and 38 children. If half of the passengers get off the plane at Houston, how many passengers are left on the plane?
- For **21**, use the diagram below.



- **21. a** Name a pair of parallel lines.
 - **b** What kind of lines are \overrightarrow{AF} and \overrightarrow{DH} ?

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Find the product. Estimate to check if the answer is reasonable.

1. 19.38	2. 4.25	3. 9.345	4. 7.43
<u>× 7</u>	<u>× 9</u>	<u>× 12</u>	<u>× 10</u>
5. 0.076	6. 0.0089	7. 23.89	8. 12.0005
× 9	<u>× 100</u>	× 6	<u>× 1,000</u>

Find the quotient. Estimate to check if the answer is reasonable.

9. 5)7.75	10. 4.35 ÷ 5	11. 3)10.53	12. 9.24 ÷ 6
13. 8)8.24	14. 0.08 ÷ 4	15. 3)12.48	16. 28.56 ÷ 2
17. 1.28 ÷ 8	18. 2)15.42	19. 60.06 ÷ 6	20. 9)28.8

Error Search Find each answer that is not correct. Write it correctly and explain the error.

21. 182	22. 4,879	23. 3,193	24. 52.03	25. 56.7
3)547	+ 236	- 3,094	+ 21.67	× 2.1
	4,643	101	73.70	11.907

Number Sense

Estimating and Reasoning Write whether each statement is true or false. Explain your reasoning.

- **26.** The product of 50×8.58 is between 400 and 450.
- **27.** The sum of 45.69 and 10.92 is 0.08 less than 56.69.
- **28.** The expression $18 6 + 5 \times 2$ equals 34.
- **29.** The quotient of 3,216 \div 8 is 2 more than 400.
- **30.** The expression $\frac{10k}{5}$ equals 12 when k = 6.
- **31.** The quotient 15.89 ÷ 2 is greater than 8.

Practice



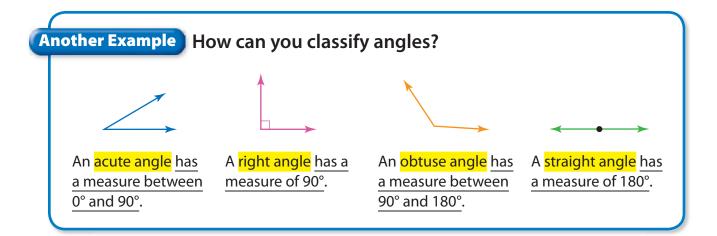
MG 2.1 Measure, identify, and draw angles, perpendicular and parallel lines, rectangles, and triangles by using appropriate tools (e.g., straightedge, ruler, compass, protractor, drawing software).

Measuring and Classifying Angles

How can you measure an angle?

An angle is formed by two rays that have the same endpoint. The common endpoint is called the vertex (plural: vertices.)

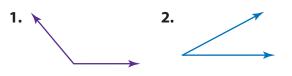
Angle *ABC* is shown above to the right. We write this as $\angle ABC$. It can also be named $\angle CBA$ or just $\angle B$.



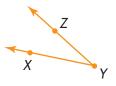
Guided Practice*

Do you know HOW?

In 1 and 2, measure and classify each angle.



3. Reasoning Give three different names for this angle. Identify the vertex and sides.



Do you UNDERSTAND?

4. In the figure below, how many angles are formed? What are their measures? Are the angles acute, right, or obtuse?

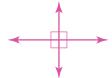
Hends-On

protractor

vertex

R

sides



 Draw an obtuse angle. Label it with 3 points and the angle measure.

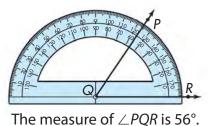




To measure an angle

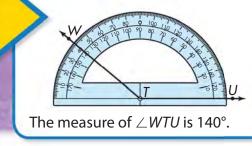
You use a <mark>protractor</mark> <u>to measure and draw angles</u>. <u>Angles are measured in <mark>degrees</mark>. It takes 90° to fill a</u> square corner.

Place the protractor's center on the angle's vertex. Place the 0° mark on one side of the angle. Read the measure where the other side of the angle crosses the protractor.



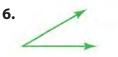
To draw an angle of 140°

Draw \overrightarrow{TU} . Be sure to label the endpoint *T*. Place the protractor's center on *T*. Line up \overrightarrow{TU} with the 0° mark. Place a point at 140°. Label it *W*. Draw \overrightarrow{TW} .



Independent Practice

In **6** through **8**, classify each angle as acute, right, obtuse, or straight. Then measure each angle.





In **9** through **12**, draw the angles with a protractor. Classify the angles as acute, right, or obtuse.

9. 35° **10.** 110° **11.** 90° **12.** 76°

Problem Solving

- **13. Reasoning** If \overrightarrow{CB} is perpendicular to \overrightarrow{CD} , then $\angle BCD$ is
 - **A** an acute angle. **C** an obtuse angle.
 - **B** a right angle.
- **D** a straight angle.
- 15. Angles can be found on the world's largest basket. What kind of angle is ∠ADC? ∠CBD? ∠ADB?



- 14. For his birthday, John received the same amount of money from each of his 10 friends, plus \$20 from his brother. If John received a total of \$120, how much did each friend give him?
- **16. Writing to Explain** Carlos says that two times the measure of an acute angle will always equal the measure of an obtuse angle. Is he right? Give examples to explain your answer.





MG 2.0 Identify, describe, and classify the properties of, and the relationships between, plane and solid geometric figures.

Polygons

How do you name a polygon?

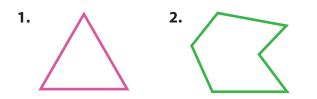
A <mark>polygon</mark> is a <u>closed plane figure</u> made up of line segments.

A regular polygon has sides of equal length and angles of equal measure.

Guided Practice*

Do you know HOW?

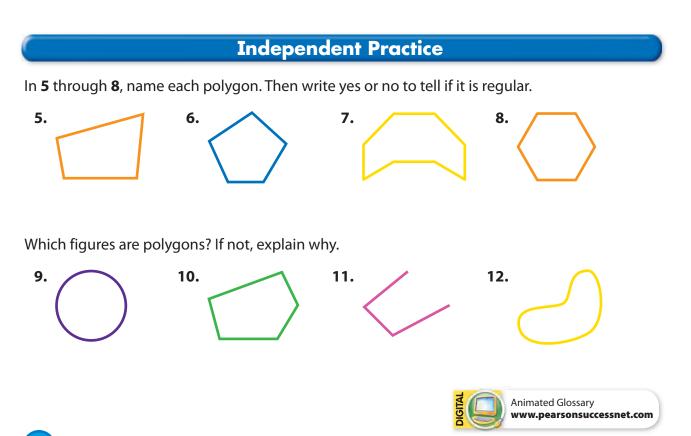
Name the polygon and classify it as regular or irregular.



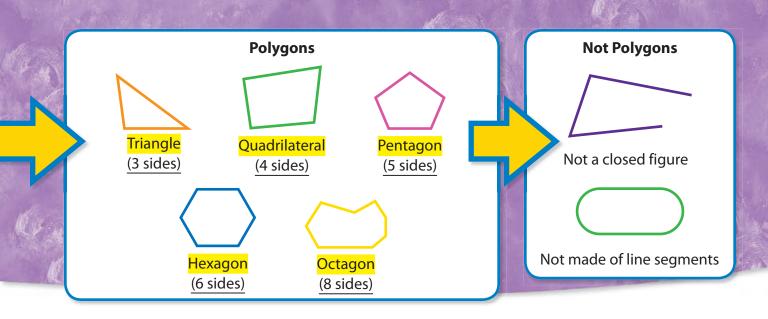
Do you UNDERSTAND?

- 3. How many sides and how many vertices does a pentagon have? A hexagon?
- **4.** What type of polygon does each road sign in the example at the top appear to be? Which one is a regular polygon?

STOP



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Problem Solving

For 13, use the picture below.

13. What kinds of polygons can you find in the architecture of the Palace of Fine Arts in San Francisco, California?



15. After a party, there was one pizza left. It was divided into 8 pieces. Kip shared it equally among 4 friends. Which shows how many pieces each friend got?

A	8	C 4	
В	6	D 2	

18. Think About the Process Juanita's car gets 28 miles per gallon. Which expression shows how many gallons it will take to drive 720 miles?

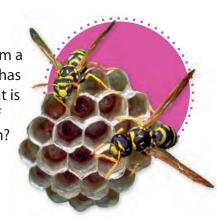
A 720 × 28 C	720 + 28
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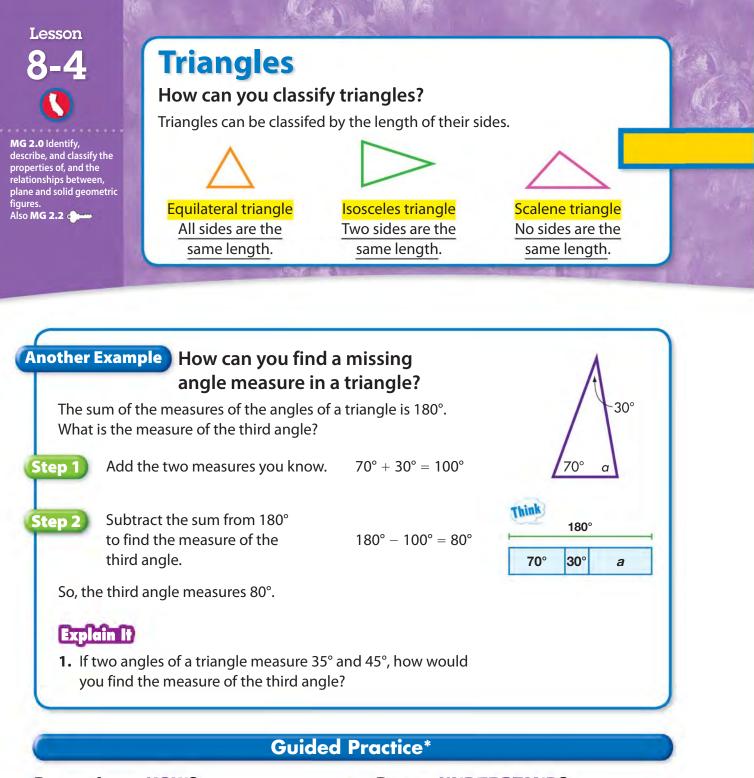
B 720 \div 28 **D** 720 - 28

14. While driving, Shania saw a No Passing Zone sign and an Interstate Highway sign. Are these polygons? If so, are they regular?



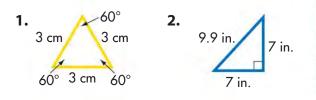
- **16.** If each side of a regular pentagon equals 4 feet, what is its perimeter?
- 17. Divide a square in half by connecting two vertices. What type polygons are formed? Are they regular or irregular?
- **19.** Each cell from a wasps' hive has 6 sides. What is the name of this polygon?





Do you know HOW?

Classify each triangle by its sides and then by its angles.

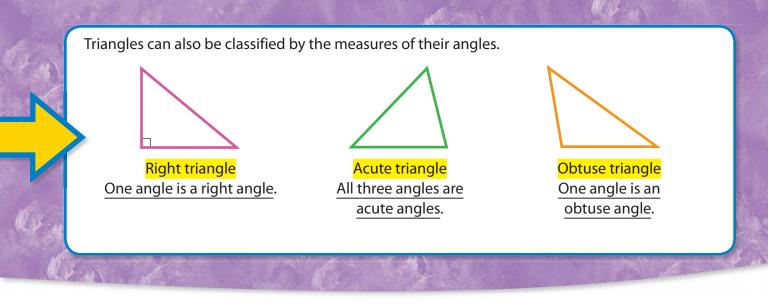


Do you UNDERSTAND?

- **3.** Can a right triangle have an obtuse angle in it? Why or why not?
- **4.** Can an equilateral triangle have only two sides of equal length? Why or why not?

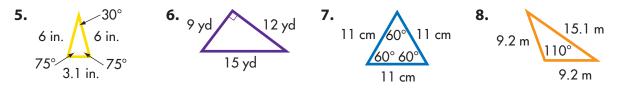






Independent Practice

Classify each triangle by its sides and then by its angles.



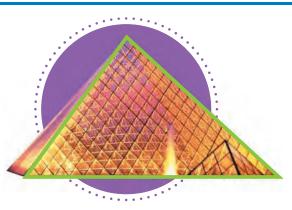
Two angle measures of a triangle are given. Find the measure of the third angle.

9. 48°, 63°	10. 90°, 40°	11. 65°, 50°	12. 130°, 24°

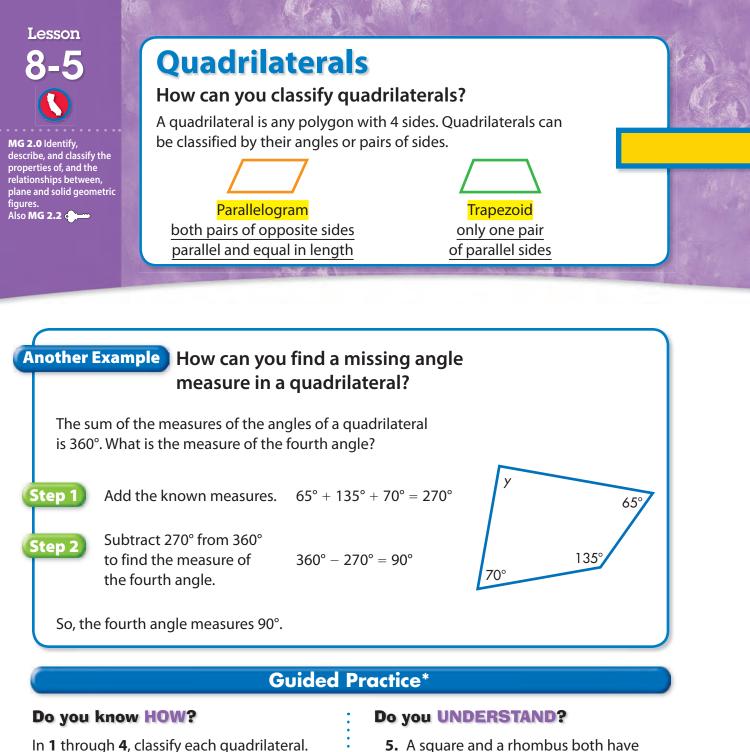
Problem Solving

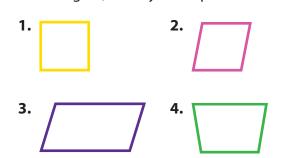
For **13**, use the picture at the right.

- **13.** The Louvre Museum is located in Paris, France. The Louvre Pyramid serves as an entrance to the museum. Classify the green triangle on the picture by the lengths of its sides and the measures of its angles.
- 14. Writing to Explain The measures of two angles of a triangle are 23° and 67°. Is the triangle acute, right, or obtuse? Use geometric terms in your explanation.



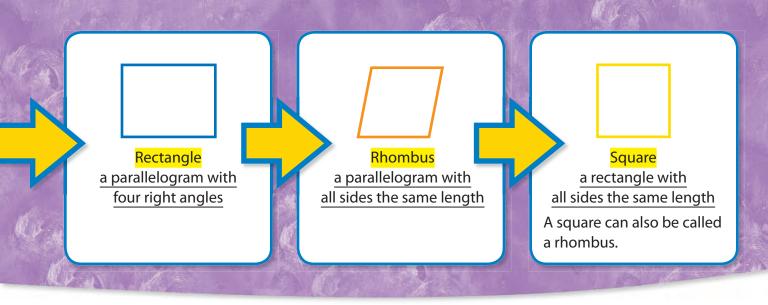
15. Strategy Focus During a sale at the bookstore, books sold for \$3 and magazines sold for \$2.50. Jan spent \$16 and bought a total of 6 books and magazines. How many of each did she buy? Use Try, Check, and Revise.





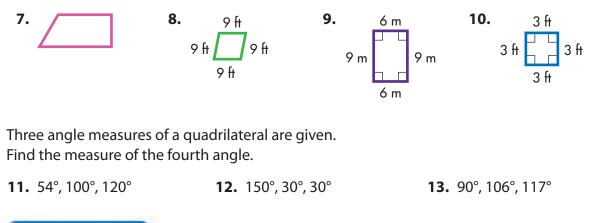
- A square and a rhombus both have four sides that are equal in length. How can you tell the difference between the two quadrilaterals?
- 6. Writing to Explain Why can a rectangle also be called a parallelogram?





Independent Practice

Classify each quadrilateral.



Problem Solving

- **14.** Which quadrilateral never has 4 equal sides?
 - **A** Square **C** Rectangle
 - **B** Trapezoid **D** Rhombus
- **15.** Draw a quadrilateral that is not a parallelogram.
- **16.** Draw rectangle *ABCD*. Then draw a diagonal line connecting points *B* and *D*. If triangle *BCD* is a right isosceles triangle, what do you know about rectangle *ABCD*?
- **17.** Think About the Process Hot dog buns come in packages of 12. Which of the following is NOT needed to find out how much you will spend on hot dog buns?
 - A The cost of one pack of buns
- **C** The number of buns you need
- **B** The cost of the hot dogs
- **D** All of the information is necessary.

Lesson 8-6

MR 3.3 Develop generalizations of the results obtained and apply them in other circumstances. Also MR 2.4, 3.2, MG 2.0 Problem Solving

Make and Test Generalizations

A generalization or general statement can be made about a rectangle.

Make a Generalization

All rectangles can be cut in half diagonally to make two congruent triangles.

Guided Practice*

Do you know HOW?

Test the generalization and state whether it appears to be correct or incorrect. If incorrect, give an example to support why.

- 1. All even numbers have more than 2 factors.
- **2.** Two congruent equilateral triangles can be joined to make a rhombus.

Do you UNDERSTAND?

- **3.** In the exercise above, how was the conclusion reached?
- **4.** What is another generalization you can make and test about rectangles?
- **5. Write a Problem** Write a real-world problem that can be solved by making and testing a generalization.

Independent Practice

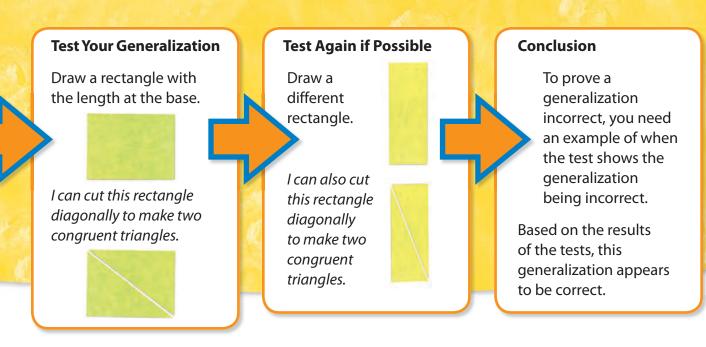
In **6** through **10**, test the generalization and state whether it appears to be correct or incorrect. If incorrect, give an example to support why.

- 6. The sum of the angles of any triangle is 180°.
- 7. Parallel lines never intersect.
- 8. Trapezoids are parallelograms.
- 9. All even numbers are composite.
- **10.** All cubes are three–dimensional.

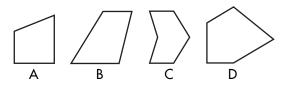


- What do I know?
- What am I asked to find?
- What diagram can I use to help understand the problem?
- Can I use addition, subtraction, multiplication, or division?
- Is all of my work correct?
- Did I answer the right question?
- Is my answer reasonable?





11. What is the same about all of these polygons?

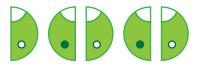


13. What is the best estimate of the shaded portion of the picture shown below?



- **15.** Mike weighs 24 more pounds than Marcus. Together, they weigh 250 pounds. How much do they each weigh?
- **17.** Marcia and Tim played Ping-Pong. Marcia won the game with a score of 21. She won by 7 points. Draw a picture and write an equation to find Tim's score.
- **18.** How many whole numbers have exactly two digits? Hint: 99 is the greatest two-digit whole number.

- **12.** One pint of blueberries contains about 80 berries. You have a fruit salad recipe that calls for 20 blueberries per serving. You have all of the other fruit necessary for the salad, but only 1 quart of blueberries. How many servings of the fruit salad can you prepare?
- **14.** Draw the next figure in the pattern shown below.



16. Find the missing numbers in each table. Then, write the rule.

а	Days	1	2	4	7
	Dollars	\$8		\$32	
b	Team	1	2	4	9



Animated Glossary www.pearsonsuccessnet.com

Test Prep

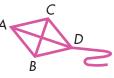
1. Which of the following correctly describes the triangles shown? (8-4)



- **A** Both triangles have a right angle.
- **B** Only one triangle has an acute angle.
- **C** Both triangles have at least two obtuse angles.
- **D** Both triangles have at least two acute angles.
- 2. A right triangle has an angle whose measure is 35°. What is the measure of the other angle in the triangle? (8-4)
 - **A** 35°
 - **B** 55°
 - **C** 72.5°
 - **D** 145°
- **3.** Which of the following can be used to describe the shape below? (8-5)

- **A** Opposite sides are perpendicular.
- **B** All angles are obtuse.
- **C** Adjacent sides are parallel.
- **D** All sides are congruent.

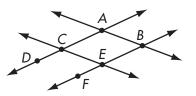
4. What is the relationship between segments *AD* and *BC*? (8-1)



- **A** They are congruent.
- B They are adjacent.
- **C** They are perpendicular.
- **D** They are parallel.
- 5. Sabra's glasses have lenses that are the shape shown in the picture below. Which of the following could NOT be used to describe the lenses? (8-3)



- A Quadrilateral
- **B** Regular polygon
- C Hexagon
- **D** Opposite sides parallel
- **6.** Which of the following appear to be parallel lines in the diagram shown? (8-1)



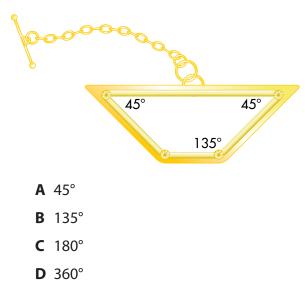
- **A** \overrightarrow{AB} and \overrightarrow{CE}
- **B** \overrightarrow{AB} and \overrightarrow{FB}
- **C** \overrightarrow{CE} and \overrightarrow{DA}
- **D** \overrightarrow{FB} and \overrightarrow{CE}

Test Prep

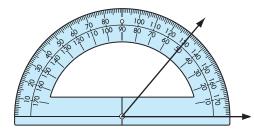
7. The figures below are rhombuses.Which generalization is incorrect, based on these figures? (8-6)



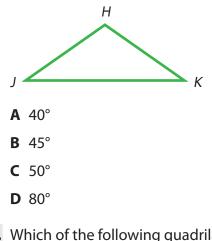
- **A** A square can be a rhombus.
- **B** A rhombus can be a square.
- **C** All rhombuses are squares.
- **D** All squares are rhombuses.
- 8. A sail on a sailboat is a triangle with two sides perpendicular and no two sides congruent. What two terms could be used to describe the sail? (8-4)
 - A Equilateral and right
 - B Right and isosceles
 - C Scalene and right
 - **D** Isosceles and acute
- **9.** How many degrees is the measure of the fourth angle in the necklace charm shown? (8-5)



10. Which of the following is closest to the measure of the angle shown? (8-2)



- **A** 40°
- **B** 50°
- **C** 130°
- **D** 140°
- **11.** Triangle *HJK* is an isosceles triangle. The measures of angles *J* and *K* are equal. The measure of angle *H* is 100°. What is the measure of angle *J*? (8-4)

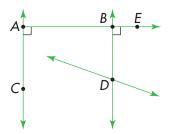


- **12.** Which of the following quadrilaterals must have all four sides of equal length? (8-5)
 - A Rhombus
 - **B** Rectangle
 - C Trapezoid
 - **D** Parallelogram

Reteaching

Set A, pages 174–176

Geometric ideas are shown in the diagram below.



Name a line segment on \overrightarrow{AE} .	ĀB
Name two perpendicular rays.	\overrightarrow{AE} and \overrightarrow{BD}
Name two parallel lines.	\overrightarrow{AC} and \overrightarrow{BD}
Name three points.	С, В, А

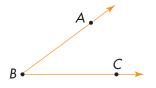
Remember that intersecting lines pass through the same point. If they form a right angle, they are perpendicular lines.

Use the figure at the left to name each of the following.

- **1.** A ray that intersects two parallel line segments.
- 2. A vertical ray.
- 3. A horizontal ray.
- **4.** A line segment that is perpendicular to two rays.

Set B, pages 178–179

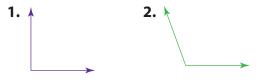
Measure the angle below with a protractor and classify it as acute, right, or obtuse.



An acute angle measures less than 90°. This angle measures 38°. So, this angle is acute.

Remember that you can compare most angles to a right angle and know whether it is greater or less than 90°, or you can measure it with a protractor.

Measure each angle with a protractor and classify it as acute, right, or obtuse.



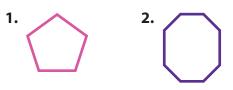
Set C, pages 180–181

Name the polygon and state whether it is regular or irregular.



The polygon has six sides that are all equal in length and angles that are equal in measure. It is a regular hexagon.

Remember that a regular polygon has sides and angles of equal length and measure.



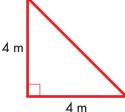


Reteaching

Set D, pages 182–183

Classify the triangle by the measure of its angles and the length of its sides.

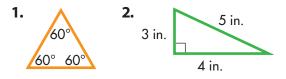
Since one of the angles is right, this is a right triangle. Since two of the sides are the same length, this is an isosceles triangle.



Using both terms, this is a right, isosceles triangle.

Remember that right, obtuse, and acute describe the angles of a triangle. Equilateral, scalene, and isosceles describe the sides of a triangle.

Classify each triangle by the size of its angles and the length of its sides.



Set E, pages 184–185

Classify the quadrilateral. Then find the missing angle measure.

The quadrilateral has two sets of parallel lines with all sides the same length. It is a rhombus. 4 cm $? \quad 60^{\circ}$ 4 cm 4 cm 4 cm

The sum of the measures of the angles in a quadrilateral is 360°.

 $360^{\circ} - (60^{\circ} + 60^{\circ} + 120^{\circ}) = 120^{\circ}$

So, the missing angle measure is 120°.

Set F, pages 186–187

Test the following generalization and state whether it appears to be correct or incorrect. If incorrect, give an example to support why.

Generalization

The sum of the angles in any rectangle is 180°.

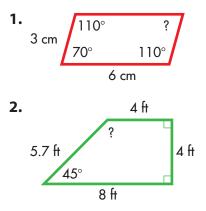
Test Your Generalization

Draw a rectangle. Notice that each of the four angles is 90°. Add to find the sum of the angles. $90^{\circ} + 90^{\circ} + 90^{\circ} = 360^{\circ}$

Conclusion

The generalization is incorrect.

Remember that the sum of the angles of a quadrilateral is 360°.



Remember to test a generalization more than once before drawing a conclusion that the generalization is true.

Test the generalization. State if it appears to be correct or not. If incorrect, give an example to support why.

1. Triangular prisms always have two bases that are equilateral triangles.